

## Bipolar Transistor Design

$$\begin{array}{ll}
 N_A \approx 6.023 \times 10^{23} \frac{1}{\text{mole}} & e \approx 1.6 \times 10^{19} \text{ coul} \\
 k_B \approx 1.38 \times 10^{-23} \frac{\text{joule}}{\text{K}} & h \approx 6.63 \times 10^{-34} \text{ J}\cdot\text{s} \\
 & m \approx 10^{-31} \text{ kg} \\
 & \epsilon_0 \approx 8.85 \times 10^{-12} \frac{\text{F}}{\text{m}} \\
 & \text{pF} \approx 10^{-9} \text{ F}
 \end{array}$$

By further integration of Poisson's equation we can show (see Question 6.3) that the contact potential  $\phi$  is given by

$$\phi = \frac{e}{2\epsilon\epsilon_0} (N_d l_n^2 + N_a l_p^2) \quad (6.6)$$

Rearranging this expression and using the relationship in eqn (6.5) we can also show (see Question 6.4) that the depletion layer width on the p-type side is

$$l_p = \left( \frac{\phi 2\epsilon\epsilon_0}{eN_a} \frac{N_d}{N_a + N_d} \right)^{1/2} \quad (6.7)$$

and that on the n-type side is

$$l_n = \left( \frac{\phi 2\epsilon\epsilon_0}{eN_d} \frac{N_a}{N_a + N_d} \right)^{1/2} \quad (6.8)$$

$$E_g \approx 1.12 \text{ eV} \quad \mu \approx 11.7 \quad \text{Properties of Silicon} \quad T \approx 298 \text{ K}$$

$$\mu_n \approx 0.14 \frac{\text{m}^2}{\text{V}\cdot\text{s}} \quad m'_e \approx 0.43 m_e \quad m'_h \approx 0.54 m_e$$

$$n_i \approx 2 \times 10^{15} \frac{1}{\text{m}^3} \quad \text{Intrinsic Conductivity} \quad n_i \approx 2.41 \times 10^{15} \frac{1}{\text{m}^3}$$

$$N_a \approx 10^{18} \frac{1}{\text{m}^3} \quad \text{Acceptor Dopant Conc. in p-doped region.}$$

$$N_d \approx 10^{18} \frac{1}{\text{m}^3} \quad \text{Donor Dopant Conc. in n-doped region.}$$

$$l_{p,D} \approx 50 \mu\text{m} \quad \text{Hole Diffusion Distance}$$

$$V_{bi} = \frac{k_B T}{e} \ln \left( \frac{N_a N_d}{n_i^2} \right)$$

$$V_{bi} = 0.31 \text{ V}$$

### Governing Equations

$$l_n = \frac{1}{2} \sqrt{\frac{D_n \tau_n}{N_a + N_d}}$$

### Depletion Thicknesses

$$l_n = 1.416 \times 10^{-5} \text{ m}$$

$$n_p = N_c \exp\left[\frac{-(E_f - E_g)}{k_B T}\right]$$

$$n_n = N_c \exp\left[\frac{(E_f - E_g)}{k_B T}\right]$$

$$p_n = N_v \exp\left[\frac{-(E_f - E_g)}{k_B T}\right]$$

$$p_p = N_v \exp\left[\frac{(E_f - E_g)}{k_B T}\right]$$

$$l_p = \frac{1}{2} \sqrt{\frac{D_p \tau_p}{N_a + N_d}}$$

$$l_p = 1.416 \times 10^{-5} \text{ m}$$

$$V_{bi} = \frac{k_B T}{e} \ln \left[ \frac{N_a N_d}{n_i^2} \right]$$

$$W = 5 \times 10^{-3} \text{ m} = 2l_p$$

$$W = 3.332 \times 10^{-5} \text{ m}$$

Width of the base section (P-doped)

$$\beta = 1 - \frac{1}{2} \frac{W^2}{l_{pD}^2}$$

$$\beta = 0.995$$

Voltage Gain = ?

$$\beta = \frac{1}{1 + \frac{W^2}{4l_{pD}^2}} = 199$$